LRI-LIX BioInfo Seminar 19/01/2017 - Palaiseau

# Finding a gene tree in a phylogenetic network

**Philippe Gambette** 





#### **Outline**

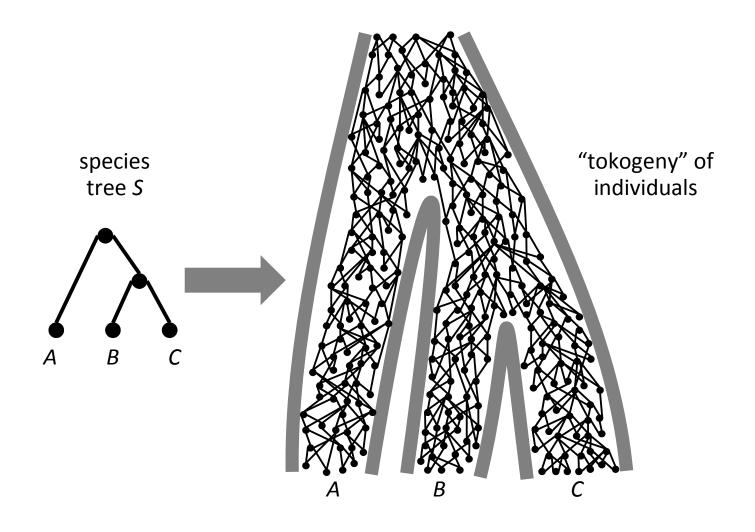
- Phylogenetic networks
- Classes of phylogenetic networks
- The Tree Containment Problem

### **Outline**

- Phylogenetic networks
- Classes of phylogenetic networks
- The Tree Contaiment Problem

### **Phylogenetic trees**

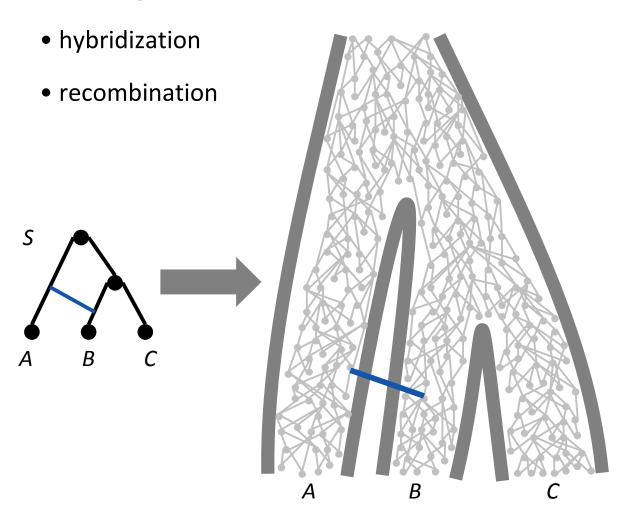
#### **Phylogenetic tree** of a set of species



### **Genetic material transfers**

**Transfers** of genetic material between coexisting species:

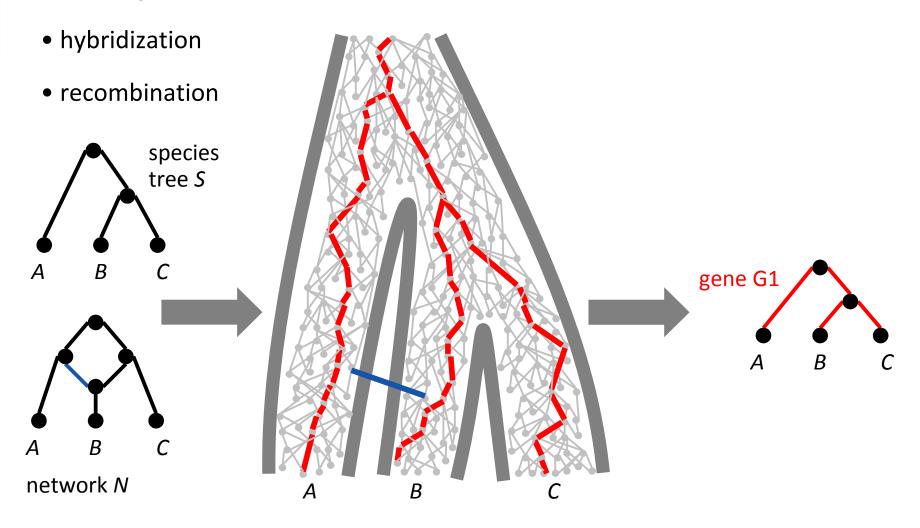
• lateral gene transfer



### **Genetic material transfers**

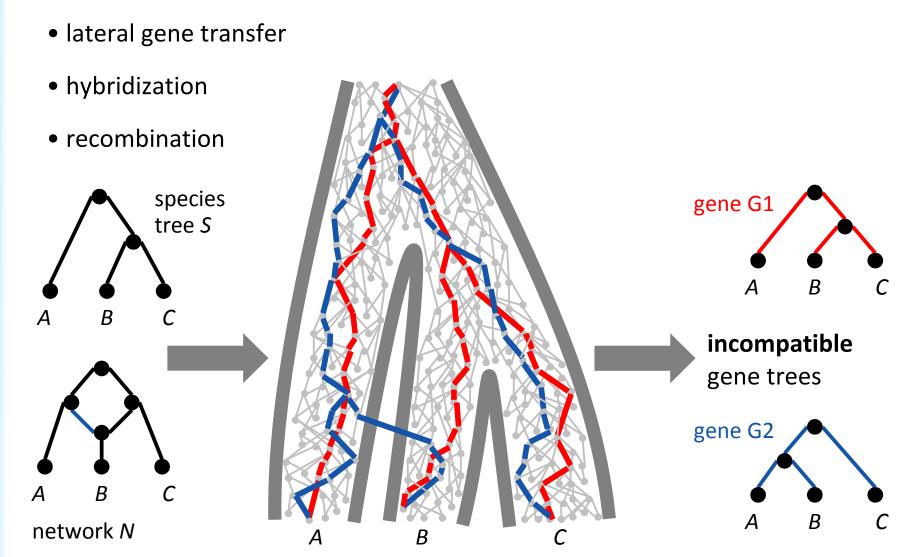
**Transfers** of genetic material between coexisting species:

• lateral gene transfer



#### **Genetic material transfers**

**Transfers** of genetic material between coexisting species:

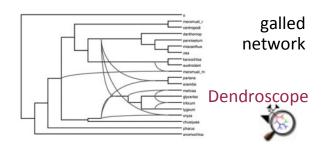


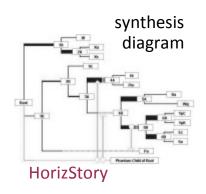
### Phylogenetic networks

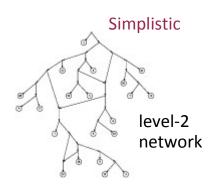
#### Phylogenetic network: network representing evolution data

• explicit phylogenetic networks

#### model evolution

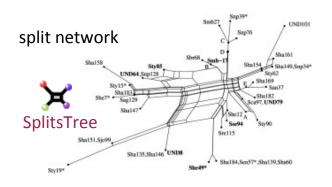


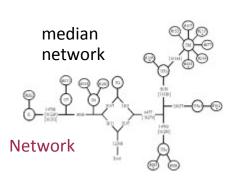




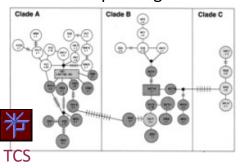
• abstract phylogenetic networks

#### classify, visualize data



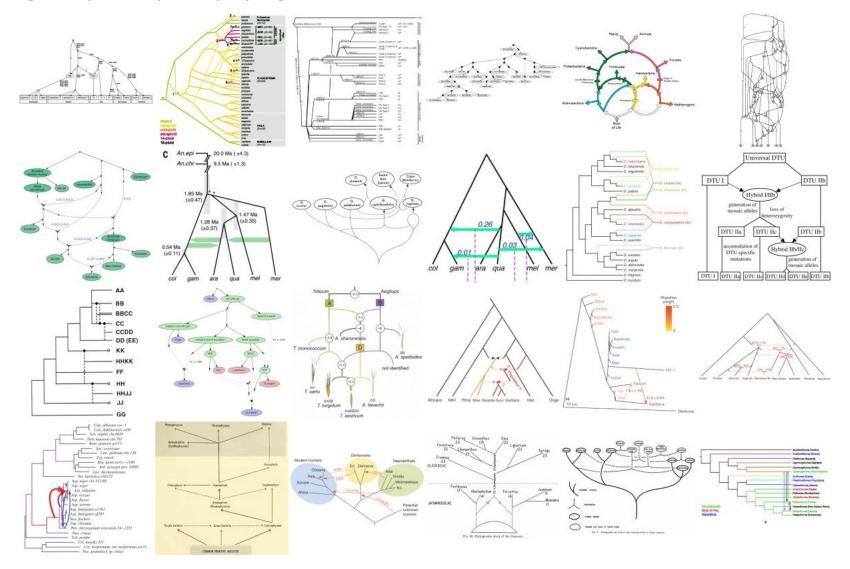


#### minimum spanning network



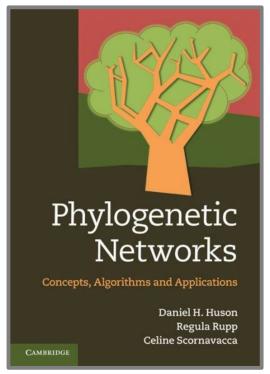
### Today: focus on explicit phylogenetic networks

#### A gallery of explicit phylogenetic networks:

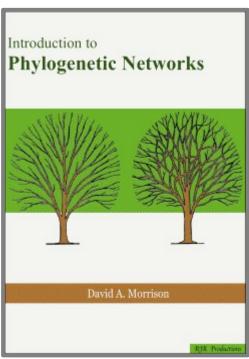


http://phylnet.univ-mlv.fr/recophync/networkDraw.php

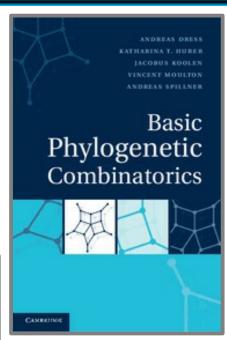
### **Books about phylogenetic networks**



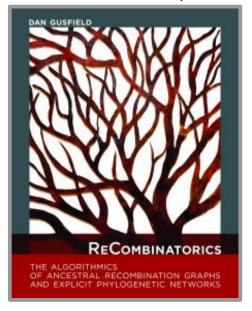
Huson, Rupp, Scornavacca, 2011 Dress, Huber, Koolen, Moulton, Spillner, 2012



Morrison, 2011



Gusfield, 2014



### Workshops about phylogenetic networks



The Future of Phylogenetic Networks, 15-19 October **2012**, Lorentz Center, Leiden, The Netherlands

Utilizing Genealogical
Phylogenetic Networks in
Evolutionary Biology:
Touching the Data,
7-11 July **2014**, Lorentz Center,
Leiden, The Netherlands



The Phylogenetic Network
Workshop, 27 - 31 Jul **2015**,
Institute for Mathematical Science
(National University of Singapore)

# Who is Who in Phylogenetic Networks

Authors Community Keywords Publications Software Browse Basket Account Contribute! About Help A Q

## FIND EXPERTS

Find researchers working on a specific topic, in a given country, and find where (journals, conferences) the community publishes or meets.

# EXPLORE RESEARCH

Browse publications, access keyword definitions and find trends in publications on phylogenetic network methods and methodologies.

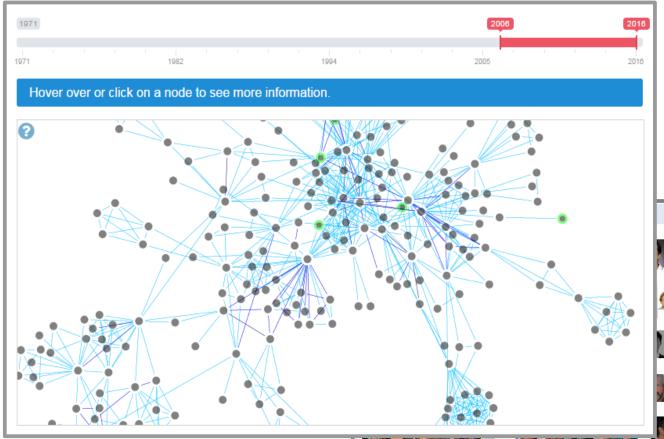
#### DISCOVER SOFTWARE

Locate programs to compute, evaluate, compare or visualize phylogenetic networks, and view how these are linked with each other and input data.

# FOLLOW COMMUNITY

Follow an author, publications tagged with a keyword, or the entire database using the a icon in the menu, on an author's page, or on a keyword's page.

Based on BibAdmin by Sergiu Chelcea + tag clouds, date histograms, journal lists, keyword definitions, co-author graphs



Who is Who in Phylogenetic Networks, Articles, **Authors** & Programs

Analysis of the co-author and keyword graphs: internship of **Tushar Agarwal** 

Agarwal, Gambette & Morrison, arXiv, 2017



```
abstract-network(88) agreement-forest(29) approximation(18) APX-hard(4) ARG(6) bayesian(4) block-realization(1)
 bootstrap(4) bound(4) branch-and-bound(1) cactus-graph(1) characterization(11) circular-split-system(13) clustering(3) coalescent(10)
 consensus(8) consistency(2) cophylogeny(1) counting(3) database(1) distance-between-networks(30) diversity(5) duplication(33)
dynamic-programming(10) enumeration(4) evaluation(25) explicit-network(191) exponential-algorithm(6) FPT(31)
from-clusters(16) from-continuous-characters(1) from-distances(45) from-gene-order(1) from-multilabeled-tree(9) from-
network(39) from-NGS-data(1) from-quartets(16) from-rooted-trees(122) from-sequences(51) from-
species-tree(46) from-splits(13) from-trees(7) from-triplets(24) from-unrooted-trees(16) galled-network(7)
galled-tree(38) generation(12) haplotype-network(2) haplotyping(1) heuristic(32) HMM(2) hybridization(52) inapproximability(5)
integer-linear-programming(3) isomorphism(3) k-reticulated(1) kernelization(2) labeling(4) lateral-gene-transfer(56) level-k-
phylogenetic-network(30) likelihood(16) lineage-sorting(10) loss(16) MASN(4) median-network(16) Median-Joining(2) Minimal-
lateral-network(1) minimum-contradiction(2) minimum-number(33) minimum-spanning-network(2) model-selection(2) mu-distance(2)
NeighborNet(14) nested-network(2) netting(3) normal-network(9) NP-complete(33) optimal-realization(3) parsimony(39)
                                                                                phylogenetic-network(402) phylogeny(387) polynomial(70)
 population-genetics(5) Program-AdmixTools(1) Program-ALE(1) Program-Angst(2) Program-Arlequin(5) Program-Beagle(3) Program-BIMLR(1) Program-
 Bio-PhyloNetwork(4) Program-Clustistic(2) Program-CMPT(1) Program-CombineTrees(2) Program-ConsensusNetwork(1) Program-constNJ(1) Program-
 CycleKiller(3) Program-Dendroscope(14) Program-EEEP(3) Program-FastHN(1) Program-FlatNJ(1) Program-Fylogenetica(2) Program-GalledTree(1)
 Program-GraphDTL(2) Program-HapBound(1) Program-HGT_simul(1) Program-HiDe(1) Program-HorizStory(2) Program-Hybrid-Lambda(1) Program-
HybridInterleave(5) Program-HybridNET(2) Program-HybridNumber(3) Program-Hybroscale(3) Program-JML(1) Program-LatTrans(5) Program-
LEV1ATHAN(1) Program-Lev1Generator(1) Program-Level2(2) Program-lingpy(1) Program-LNetwork(2) Program-Marlon(3) Program-Marlon(3) Program-Marlon(3)
Net(1) Program-McKiTscH(1) Program-Mowgli(5) Program-MowgliNNI(2) Program-MPNet(1) Program-MY-CLOSURE(1) Program-Nepal(7) Program-Nepal(7) Program-Nepal(7) Program-Nepal(7) Program-Nepal(8) Pro
NetGen(3) Program-NetView(1) Program-Network(5) Program-Notung(1) Program-PADRE(7) Program-Phangorn(2) Program-
PhippsNetwork(2) Program-PhyloNet(11) Program-PhyloNet-HMM(1) Program-PIRN(3) Program-Prunier(2) Program-Pyramids(3) Program-QNet(4)
 Program-Quartet(1) Program-Quartet-Decomposition(1) Program-QuartetMethods(1) Program-QuartetNet(2) Program-QuartetOecomposition(1) Program-QuartetOecomposition(1) Program-QuartetOecomposition(1) Program-QuartetOecomposition(1) Program-QuartetOecomposition(1) Program-QuartetOecomposition(2) Program-QuartetOecomposition(3) Program-QuartetOecomposition(3) Program-QuartetOecomposition(3) Program-QuartetOecomposition(3) Program-QuartetOecomposition(3) Program-QuartetOecomposition(4) Program-QuartetOecomposition(4) Program-QuartetOecomposition(5) Program-QuartetOecomposition(6) Program-QuartetOecompositi
 Program-RANGER-DTL(4) Program-RecMin(1) Program-Recodon(3) Program-RecPars(1) Program-Reticlad(2) Program-SAGE(2) Program-SAGE(1)
Program-Serial-NetEvolve(1) Program-SHRUB(3) Program-Simplistic(3) Program-Sliding-MinPD(1) Program-SNSA(2) Program-Spectronet(4) Program-Spectronet(4) Program-Spectronet(4) Program-Spectronet(4) Program-Spectronet(4) Program-Spectronet(5) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(6) Program-Spectronet(7) Program-Spectronet(7) Program-Spectronet(7) Program-Spectronet(8) Pr
SplitsTree(36) Program-SPNet(5) Program-SPRDist(1) Program-SuperQ(1) Program-T-REX(13) Program-TCS(8) Program-TERA(2) Program-SPNet(5) Program
TerminusEst(2) Program-TreeFix-DTL(1) Program-TreeMix(1) Program-Treevolve(2) Program-TripNet(2) Program-Ultra-Net(1) Program-Ultra-Net(1) Program-Ultra-Net(1) Program-Ultra-Net(1) Program-Tree-Fix-DTL(1) Program-Tree-Fix-
WeakHierarchies(2) Program-Xscape(1) pyramid(8) quasi-median-network(3) realization(4) recombination(29) recombination-detection(4)
reconstruction(255) regular-network(7) reticulogram(10) serial-evolutionary-networks(1) simulated-annealing(4) simulation(5)
site-consistency(1) software(66) split(27) split-decomposition(13) split-network(54) SPR-distance(13) spread(2)
statistical-model(32) statistical-parsimony(3) supernetwork(4) Survey(31) tanglegram(1) time-consistent-network(12) tree-child-
network(15) tree-sibling-network(10) tripartition-distance(9) triplet-distance(3) unicyclic-network(3) visualization(30) weak-
hierarchy(8) weakly-compatible(3)
```

```
abstract-network(88) agreement-forest(29) approximation(18) APX-hard(4) ARG(6) bayesian(4) block-realization(1)
  bootstrap(4) bound(4) branch-and-bound(1) cactus-graph(1) characterization(11) circular-split-system(13) clustering(3) coalescent(10)
  consensus(8) consistency(2) cophylogeny(1) counting(3) database(1) distance-between-networks(30) diversity(5) duplication(33)
 dynamic-programming(10) enumeration(4) evaluation(25) explicit-network(191) exponential-algorithm(6) FPT(31)
from-clusters(16) from-continuous-characters(1) from-distances(45) from-gene-order(1) from-multilabeled-tree(9)
network(39) from-NGS-data(1) from-quartets(16) from-rooted-trees(122) from-sequences(51) from-
 species-tree(46) from-splits(13) from-trees(7) from-triplets(24) from-unrooted-trees(16) galled-network(7)
  galled-tree(38) generation(12) haplotype-network(2) haplotyping(1) heuristic(32) HMM(2) hybridization(52) inapproximability(5)
 integer-linear-programming(3) isomorphism(3) k-reticulated(1) kernelization(2) labeling(4) lateral-gene-transfer(56) level-k-
 phylogenetic-network(30) likelihood(16) lineage-sorting(10) loss(16) MASN(4) median-network(16) MedianJoining(2) Minimal-
  lateral-network(1) minimum-contradiction(2) minimum-number(33) minimum-spanning-network(2) model-selection(2) mu-distance(2)
  NeighborNet(14) nested-network(2) netting(3) normal-network(9) NP-complete(33) optimal-realization(3) parsimony(39)
                                                                                                        phylogenetic-network(402) phylogeny(387)
 population-genetics(5) Program-AdmixTools(1) Program-ALE(1) Program-Angst(2) Program-Arlequin(5) Program-Beagle(3) Program-BIMLR(1) Program-
 Bio-PhyloNetwork(4) Program-Clustistic(2) Program-CMPT(1) Program-CombineTrees(2) Program-ConsensusNetwork(1) Program-constNJ(1) Program-constNJ(1
 CycleKiller(3) Program-Dendroscope(14) Program-EEEP(3) Program-FastHN(1) Program-FlatNJ(1) Program-Fvlogenetica(2) Program-GalledTree(1)
Program-GraphDTL(2) Program-HapBound(1) Program-HGT_simul(1) Program-HiDe(1) Program-HorizStory(2) Program-Hybrid-Lambda(1) Program-HorizStory(2) Program-HorizStory(2) Program-HorizStory(2) Program-HorizStory(2) Program-HorizStory(2) Program-HorizStory(3) Program-
 HybridInterleave(5) Program-HybridNET(2) Program-HybridNumber(3) Program-Hybroscale(3) Program-JML(1) Program-LatTrans(5) Program-
 LEV1ATHAN(1) Program-Lev1Generator(1) Program-Level2(2) Program-lingpy(1) Program-Levtwork(2) Program-Marlon(3) Program-Marlon(3) Program-Marlon(3)
Net(1) Program-MckTscH(1) Program-Mowgli(5) Program-MowgliNNI(2) Program-MPNet(1) Program-MY-CLOSURE(1) Program-Nepal(7) Program-Nepal(7) Program-Nepal(7) Program-Nepal(8) Prog
 NetGen(3) Program-NetView(1) Program-Network(5) Program-Notung(1) Program-PADRE(7) Program-Phangorn(2) Program-Network(5) Program-Notung(1) Program-Notung(1
PhippsNetwork(2) Program-PhyloNet(11) Program-PhyloNet-HMM(1) Program-PIRN(3) Program-Prunier(2) Program-Pyramids(3) Program-QNet(4)
Program-Quartet(1) Program-QuartetDecomposition(1) Program-QuartetMethods(1) Program-QuartetNet(2) Program-QuartetDecomposition(1) Program-QuartetDecomposition(1) Program-QuartetDecomposition(1) Program-QuartetDecomposition(1) Program-QuartetDecomposition(2) Program-QuartetDecomposition(3) Program-QuartetDecomposition(3) Program-QuartetDecomposition(3) Program-QuartetDecomposition(3) Program-QuartetDecomposition(3) Program-QuartetDecomposition(3) Program-QuartetDecomposition(4) Program-QuartetDecomposition(5) Program-QuartetDecomposition(6) Program-QuartetDecompositio
  Program-RANGER-DTL(4) Program-RecMin(1) Program-Recodon(3) Program-RecPars(1) Program-Reticlad(2) Program-SAGE(2) Program-SAQ-Net(1)
  Program-Serial-NetEvolve(1) Program-SHRUB(3) Program-Simplistic(3) Program-Sliding-MinPD(1) Program-SNSA(2) Program-Spectronet(4) Program-S
 SplitsTree(36) Program-SPNet(5) Program-SPRDist(1) Program-SuperQ(1) Program-T-REX(13) Program-TCS(8) Program-TERA(2) Program-T-REX(13) Pr
 TerminusEst(2) Program-TreeFix-DTL(1) Program-TreeMix(1) Program-Treevolve(2) Program-TripNet(2) Program-Ultra-Net(1) Program-Ultra-Net(1) Program-Treevolve(2) Program-Treevolve(3) Program-Treevolve(4) Program-Treevolve(5) Program-Treevolve(6) Program-Treevolve(6) Program-Treevolve(7) Program-Treevolve(8) Program-Treevolve(8) Program-Treevolve(8) Program-Treevolve(8) Program-Treevolve(9) Program-Treevolve
  WeakHierarchies(2) Program-Xscape(1) pyramid(8) quasi-median-network(3) realization(4) recombination(29) recombination-detection(4)
reconstruction(255) regular-network(7) reticulogram(10) serial-evolutionary-networks(1) simulated-annealing(4) simulation(5)
site-consistency(1) software(66) split(27) split-decomposition(13) split-network(54) SPR-distance(13) spread(2)
statistical-model(32) statistical-parsimony(3) supernetwork(4) Survey(31) tanglegram(1) time-consistent-network(12) tree-child-
 network(15) tree-sibling-network(10) tripartition-distance(9) triplet-distance(3) unicyclic-network(3) visualization(30) weak-
  hierarchy(8) weakly-compatible(3)
```

input

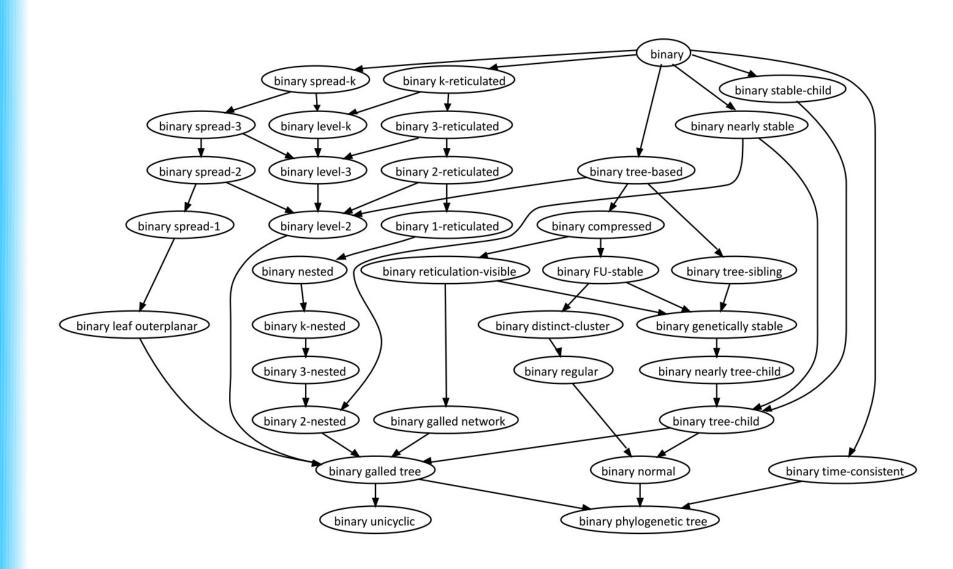
software

```
abstract-network(88) agreement-forest(29) approximation(18) APX-hard(4) ARG(6) bayesian(4) block-realization(1)
bootstrap(4) bound(4) branch-and-bound(1) cactus-graph(1) characterization(11) circular-split-system(13) clustering(3) coalescent(10)
consensus(8) consistency(2) cophylogeny(1) counting(3) database(1) distance-between-networks(30) diversity(5) duplication(33)
dynamic-programming(10) enumeration(4) evaluation(25) explicit-network(191) exponential-algorithm(6) FPT(31)
from-clusters(16) from-continuous-characters(1) from-distances(45) from-gene-order(1) from-multilabeled-tree(9)
                                                                                                                                input
network(39) from-NGS-data(1) from-quartets(16) from-rooted-trees(122) from-sequences(51)
species-tree(46) from-splits(13) from-trees(7) from-triplets(24) from-unrooted-trees(16) galled-network(7)
qalled-tree(38) generation(12) haplotype-network(2) haplotyping(1) heuristic(32) HMM(2) hybridization(52) inapproximability(5)
integer-linear-programming(3) isomorphism(3) k-reticulated(1) kernelization(2) labeling(4) lateral-gene-transfer(56) level-k-
phylogenetic-network(30) likelihood(16) lineage-sorting(10) loss(16) MASN(4) median-network(16) MedianJoining(2) Minimal-
                 minimum-contradiction(2) minimum-number(33) minimum-spanning-network(2)
                   nested-network(2) netting(3) normal-network(9) NP-complete(33)
NeighborNet(14)
                                                                                       optimal-realization(3) parsimony(39)
                        phylogenetic-network(402)
population-genetics(5) Program-AdmixTools(1) Program-ALE(1) Program-Angst(2) Program-Arlequin(5) Program-Beagle(3) Program-BIMLR(1) Program-
Bio-PhyloNetwork(4) Program-Clustistic(2) Program-CMPT(1) Program-CombineTrees(2) Program-ConsensusNetwork(1) Program-constNJ(1) Program-
CycleKiller(3) Program-Dendroscope(14) Program-EEEP(3) Program-FastHN(1) Program-FlatNJ(1) Program-Fylogenetica(2) Program-GalledTree(1)
                                                                                                                                software
Program-GraphDTL(2) Program-HapBound(1) Program-HGT_simul(1) Program-HiDe(1) Program-HorizStory(2) Program-Hybrid-Lambda(1)
HybridInterleave(5) Program-HybridNET(2) Program-HybridNumber(3) Program-Hybroscale(3) Program-JML(1) Program-LatTrans(5) Program-
LEV1ATHAN(1) Program-Lev1Generator(1) Program-Level2(2) Program-lingpy(1) Program-LNetwork(2) Program-MaafB(2) Program-Marlon(3) Program-Mc-
Net(1) Program-MckTscH(1) Program-Mowgli(5) Program-MowgliNNI(2) Program-MPNet(1) Program-MY-CLOSURE(1) Program-Nepal(7) Program-Nepal(7)
NetGen(3) Program-NetView(1) Program-Network(5) Program-Notung(1) Program-PADRE(7) Program-Phangorn(2) Program-
PhippsNetwork(2) Program-PhyloNet(11) Program-PhyloNet-HMM(1) Program-PIRN(3) Program-Prunier(2) Program-Pyramids(3) Program-QNet(4)
Program-Quartet(1) Program-Quartet-Decomposition(1) Program-QuartetMethods(1) Program-QuartetNet(2) Program-QuasiDec(1) Program-QuickCass(1)
Program-RANGER-DTL(4) Program-RecMin(1) Program-Recodon(3) Program-RecPars(1) Program-Reticlad(2) Program-SAGE(2) Program-SAQ-Net(1)
Program-Serial-NetEvolve(1) Program-SHRUB(3) Program-Simplistic(3) Program-Sliding-MinPD(1) Program-SNSA(2) Program-Spectronet(4) Program-S
SplitsTree(36) Program-SPNet(5) Program-SPRDist(1) Program-SuperQ(1) Program-T-REX(13) Program-TCS(8) Program-TERA(2) Program-
TerminusEst(2) Program-TreeFix-DTL(1) Program-TreeMix(1) Program-Treevolve(2) Program-TripNet(2) Program-ultra-Net(1) Program-Ultranet(1) Program-
WeakHierarchies(2) Program-Xscape(1) pyramid(8) quasi-median-network(3) realization(4) recombination(29) recombination-detection(4)
reconstruction(255) regular-network(7) reticulogram(10) serial-evolutionary-networks(1) simulated-annealing(4) simulation(5)
site-consistency(1) software(66) split(27) split-decomposition(13) split-network(54) SPR-distance(13) spread(2)
                                                                                                                                classes
statistical-model(32) statistical-parsimony(3) supernetwork(4) Survey(31) tanglegram(1) time-consistent-network(12) tree-child-
network(15) tree-sibling network(10) tripartition-distance(9) triplet-distance(3) unicyclic-network(3) visualization(30)
hierarchy(8) weakly-compatible(3
```

### **Outline**

- Phylogenetic networks
- Classes of phylogenetic networks
- The Tree Contaiment Problem

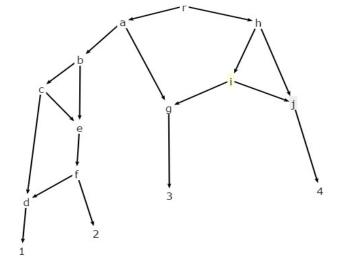
### Classes of phylogenetic networks



joint work with Maxime Morgado and Narges Tavassoli http://phylnet.univ-mlv.fr/isiphync/

binary	unio	gall	tree	nea	gall	gen	<u>reti</u>	tree	con	non	regi	dist	FU-	nea	tree	nes	<u>2-n</u>	<u>3-n</u> (	leve	leve	leaf	spri	spn	spr	tim
unicyclic	=	c	_	C	_	_	C	_	_	<u>5</u>	<u>5</u>	<u>5</u>	C	_	_	_	<b>C</b>	C	_	C	C	_	_	_	<u>5</u>
galled tree	<u>6</u>	=	_	_	_	_	_	_	_	<u>5</u>	<u>5</u>	<u>5</u>	_	_	_	_	_	_	C	_	C	_	_	_	<u>5</u>
tree-child	<u>6</u>	7	=	_	C	_	_	<b>C</b>	_	<u>5</u>	<u>5</u>	<u>5</u>	_	C	<b>C</b>	7	7	7	<u>15</u>	<u>15</u>	7	7			<u>5</u>
nearly tree-child	<u>6</u>	7	8	=	8	C	_	_	_	<u>5</u>	<u>5</u>	<u>5</u>	_	8	_	7	7	7	8	<u>15</u>	7	7			<u>5</u>
galled network	2	2	1	1	=	1	_	1	_	1	1	1	<u>14</u>	<u>21</u>	_	7	7	7	<u>18</u>	<u>18</u>	7	7			<u>5</u>
genetically stable	4	4	4	4	4	=	_	_	_	<u>5</u>	<u>5</u>	<u>5</u>	_	8	_	4	4	4	8	<u>15</u>	7	7			4
reticulation-visibl	2	2	1	1	4	1	=	1	_	1	1	1	<u>14</u>	8	_	4	4	4	8	<u>15</u>	7	7			4
tree-sibling	4	4	4	4	4	<u>12</u>	<u>12</u>	=	<u>12</u>	<u>5</u>	<u>5</u>	<u>5</u>	<u>12</u>	8	_	4	4	4	8	<u>15</u>	7	7			4
compressed	2	2	1	1	4	1	<u>11</u>	1	=	1	1	1	14	8	_	4	4	4	8	<u>15</u>	7	7			4
normal	7	7	_	_	<u>13</u>	_	_	_	_	=	C	_	_	_	_	7	7	7	<u>15</u>	<u>15</u>	7	7			22
regular	2	2	2	2	<u>13</u>	2	<u>24</u>	2	_	2	=	_	_	8	_	7	7	7	8	<u>15</u>	7	7			<u>22</u>
distinct-cluster	2	2	2	2	<u>13</u>	2	<u>24</u>	2	_	2	9	=	_	8	_	7	7	7	8	<u>15</u>	7	7			22
FU-stable	2	2	1	1	4	1	<u>11</u>	1	_	1	1	1	=	8	_	4	4	4	8	<u>15</u>	7	7			4
nearly stable	2	2	2	2	3	2	<u>3</u>	2	3	2	3	3	<u>3</u>	=	3	7	7	7	3	<u>15</u>	<u>3</u>	3			<u>5</u>
tree-based	2	2	1	1	4	1	<u>12</u>	1	<u>12</u>	1	1	1	<u>12</u>	8	=	4	4	4	8	<u>15</u>	7	7			4
nested	<u>3</u>	3	<u>3</u>	3	<u>3</u>	3	<u>3</u>	<u>3</u>	<u>3</u>	3	3	<u>3</u>	<u>3</u>	<u>19</u>	3	=	<u>20</u>	<u>20</u>	3	<u>16</u>	<u>3</u>	<u>3</u>			<u>5</u>
2-nested	3	3	<u>3</u>	3	<u>3</u>	3	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<b>C</b>	3	_	=	_	3	<u>16</u>	<u>3</u>	3			<u>5</u>
3-nested	3	3	<u>3</u>	3	3	3	3	<u>3</u>	3	3	3	3	<u>3</u>	<u>19</u>	3	_	<u>19</u>	=	3	<u>16</u>	<u>3</u>	<u>3</u>			<u>5</u>
level-2	4	4	4	4	4	<u>12</u>	<u>12</u>	<u>14</u>	<u>12</u>	4	4	4	<u>12</u>	<u>17</u>	C	4	4	4	=	C	7	7	_	_	4
level-3	2	2	2	2	3	2	3	2	3	2	3	3	3	8	3	4	4	4	3	=	3	3		C	4
leaf outerplanar	4	4	4	4	4	<u>10</u>	<u>10</u>	<u>10</u>	<u>10</u>	4	4	4	<u>10</u>	8	<u>10</u>	4	4	4	8	<u>16</u>	=	_	_	_	4
spread 1	4	4	4	4	4	<u>10</u>	<u>10</u>	<u>10</u>	<u>10</u>	4	4	4	<u>10</u>	8	<u>10</u>	4	4	4	8	<u>16</u>	9	=	_	_	4
spread 2	3	3	<u>3</u>	3	3	3	3	3	3	3	<u>3</u>	3	3	8	3	4	4	4	3	<u>16</u>	3	3	=	_	4
spread 3	3	3	3	3	3	<u>3</u>	3	3	3	3	<u>3</u>	3	3	8	3	4	4	4	3	<u>16</u>	3	3		=	4
time-consistent	<u>3</u>	<u>3</u>	<u>3</u>	3	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	8	3	7	7	7	<u>3</u>	<u>23</u>	3	3			=

binary	unio	gall	tree	nea	gall	gen	<u>reti</u>	tree	con	non	regi	dist	FU-	nea	tree	nes	<u>2-n</u>	<u>3-n</u> (	leve	leve	leaf	spri	spr	spri	tim
unicyclic	=	c	C	C	_	_	C	_	_	<u>5</u>	<u>5</u>	<u>5</u>	C	C	_	C	<b>C</b>	C	_	_	C	_	_	_	<u>5</u>
galled tree	<u>6</u>	=	C	_	_	_	_	_	_	<u>5</u>	<u>5</u>	<u>5</u>	_	_	_	_	_	_	C	_	_	_	_	_	<u>5</u>
tree-child	<u>6</u>	7	=	_	C	_	_	<b>C</b>	_	<u>5</u>	<u>5</u>	<u>5</u>	_	_	_	7	7	7	<u>15</u>	<u>15</u>	7	7			<u>5</u>
nearly tree-child	<u>6</u>	7	8	=	<u>8</u>	C	_	<b>C</b>	_	<u>5</u>	<u>5</u>	<u>5</u>	_	8	<b>C</b>	7	7	7	8	<u>15</u>	7	7			<u>5</u>
galled network	2	2	1	1	=	1	_	1	_	1	1	1	14	<u>21</u>	_	7	7	7	<u>18</u>	<u>18</u>	7	7			<u>5</u>
genetically stable	4	4	4	4	4	=	_	_	_	<u>5</u>	<u>5</u>	<u>5</u>	_	8	_	4	4	4	8	<u>15</u>	7	7			4
reticulation-visibl	2	2	1	1	4	1	=	1	C	1	1	1	<u>14</u>	8	_	4	4	4	8	<u>15</u>	7	7			4
tree-sibling	4	4	4	4	4	<u>12</u>	<u>12</u>	=	<u>12</u>	<u>5</u>	<u>5</u>	<u>5</u>	<u>12</u>	8	_	4	4	4	8	<u>15</u>	7	7			4
compressed	2	2	1	1	4	1	<u>11</u>	1	=	1	1	1	<u>14</u>	8	_	4	4	4	8	<u>15</u>	7	7			4
normal	7	7	C	_	<u>13</u>	_	_	_	_	=	_	_	_	_	_	7	7	7	<u>15</u>	<u>15</u>	7	7			22
regular	2	2	2	2	<u>13</u>	2	<u>24</u>	2	_	2	=	_	_	8	_	7	7	7	8	<u>15</u>	7	7			<u>22</u>
distinct-cluster	2	2	2	2	<u>13</u>	2	<u>24</u>	2	_	2	9	=	_	8	_	7	7	7	8	<u>15</u>	7	7			22
FU-stable	2	2	1	1	4	1	<u>11</u>	1	_	1	1	1	=	8	_	4	4	4	8	<u>15</u>	7	7			4
nearly stable	2	2	2	2	3	2	<u>3</u>	2	3	2	3	3	<u>3</u>	=	3	7	7	7	3	<u>15</u>	3	3			<u>5</u>
tree-based	2	2	1	1	4	1	<u>12</u>	1	<u>12</u>	1	1	1	<u>12</u>	8	=	4	4	4	8	<u>15</u>	7	7			4
nested	3	<u>3</u>	3	3	<u>3</u>	3	<u>3</u>	<u>3</u>	3	3	3	<u>3</u>	<u>3</u>	<u>19</u>	3	=	<u>20</u>	<u>20</u>	3	<u>16</u>	3	3			<u>5</u>
2-nested	3	3	3	3	<u>3</u>	3	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	_	3	_	=	_	3	<u>16</u>	3	3			<u>5</u>
3-nested	3	3	3	3	3	3	3	<u>3</u>	3	3	3	<u>3</u>	<u>3</u>	<u>19</u>	3	C	<u>19</u>	=	3	<u>16</u>	3	3			<u>5</u>
level-2	4	4	4	4	4	<u>12</u>	<u>12</u>	<u>14</u>	<u>12</u>	4	4	4	<u>12</u>	<u>17</u>	C	4	4	4	=	C	7	7	_	_	4
level-3	2	2	2	2	<u>3</u>	2	<u>3</u>	2	<u>3</u>	2	<u>3</u>	<u>3</u>	<u>3</u>	8	3	4	4	4	3	=	3	3		C	4
leaf outerplanar	4	4	4	4	4	<u>10</u>	<u>10</u>	<u>10</u>	<u>10</u>	4	4	4	<u>10</u>	8	<u>10</u>	4	4	4	8	<u>16</u>	=	C	_	_	4
spread 1	4	4	4	4	4	<u>10</u>	<u>10</u>	<u>10</u>	<u>10</u>	4	4	4	<u>10</u>	8	<u>10</u>	4	4	4	8	<u>16</u>	9	=	_	_	4
spread 2	3	3	3	3	3	3	<u>3</u>	<u>3</u>	3	3	3	<u>3</u>	<u>3</u>	8	3	4	4	4	3	<u>16</u>	3	3	=	_	4
spread 3	3	3	3	3	3	3	<u>3</u>	<u>3</u>	3	3	3	3	<u>3</u>	8	3	4	4	4	3	<u>16</u>	3	3		=	4
time-consistent	<u>3</u>	3	<u>3</u>	3	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	<u>3</u>	8	<u>3</u>	7	7	7	<u>3</u>	<u>23</u>	3	<u>3</u>			=



#### Classes containing this network or not

#### Classes which contain this network (with direct proof)

- <u>binary genetically stable</u>: All reticulation vertices are stable (e for leaf 2, d for leaf 1, g for leaf 3, j for leaf 4) and all have at least one parent which is stable (f, parent of d, stable for leaf 2; b, parent of e, stable for leaves 1 and 2; a, parent of g, stable for leaves 1 and 2; h, parent of j, stable for leaf 4)
- binary nearly stable: All vertices except c and i (whose unique parent is in both cases stable) are stable.
- binary level-2: Easy to check.
- · binary leaf outerplanar: Easy to check.
- binary FU-stable: Easy to check.

#### Classes which do not contain this network (with direct proof)

- <u>binary nearly tree-child</u>: Reticulation vertex g is stable but none of its parents a and i have the tree-path property.
- · binary nested: Easy to check.
- binary time-consistent: The redundant arc from b to e makes it impossible to build a time-consistent labeling of the vertices.
- binary galled network: Reticulation arc (c,e) is a common arc of reticulation cycles from b to e and from c to d.
- binary distinct-cluster: Vertices h and i both have the same cluster: {3,4}
- binary 1-reticulated: Tree vertex b can reach 2 reticulation vertices by 2 directed internally vertex-disjoint paths: d and e.

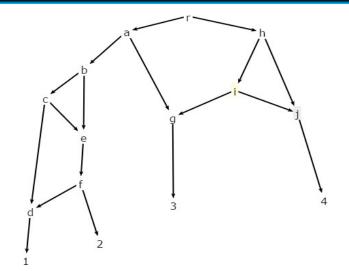
joint work with Maxime Morgado and Narges Tavassoli http://phylnet.univ-mlv.fr/isiphync/network.php?id=4

**level** = maximum number of reticulation vertices among all bridgeless components in the network

cluster = set of leaves below a vertex

#### Classes containing this network or not

#### Classes which contain this network (with direct proof)



- <u>binary genetically stable</u>: All reticulation vertices are stable (e for leaf 2, d for leaf 1, g for leaf 3, j for leaf 4) and all have at least one parent which is stable (f, parent of d, stable for leaf 2; b, parent of e, stable for leaves 1 and 2; a, parent of g, stable for leaf 4)
- binary nearly stable: All vertices except c and i (whose unique parent is in both cases stable) are stable.
- binary level-2: Easy to check.
- binary leaf outerplanar: Easy to check.
- binary FU-stable: Easy to check.

#### Classes which do not contain this network (with direct proof)

- <u>binary nearly tree-child</u>: Reticulation vertex g is stable but none of its parents a and i have the tree-path property.
- · binary nested: Easy to check.
- binary time-consistent: The redundant arc from b to e makes it impossible to build a time-consistent labeling of the vertices.
- binary galled network: Reticulation arc (c,e) is a common arc of reticulation cycles from b to e and from c to d.
- binary distinct-cluster: Vertices h and i both have the same cluster: {3,4}
- binary 1-reticulated: Tree vertex b can reach 2 reticulation vertices by 2 directed internally vertex-disjoint paths: d and e.

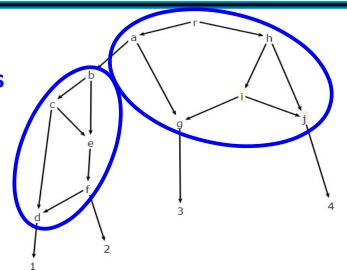
joint work with Maxime Morgado and Narges Tavassoli http://phylnet.univ-mlv.fr/isiphync/network.php?id=4

level = maximum number of reticulation
vertices among all bridgeless components
in the network

**cluster** = set of leaves below a vertex

#### Classes containing this network or not

#### Classes which contain this network (with direct proof)

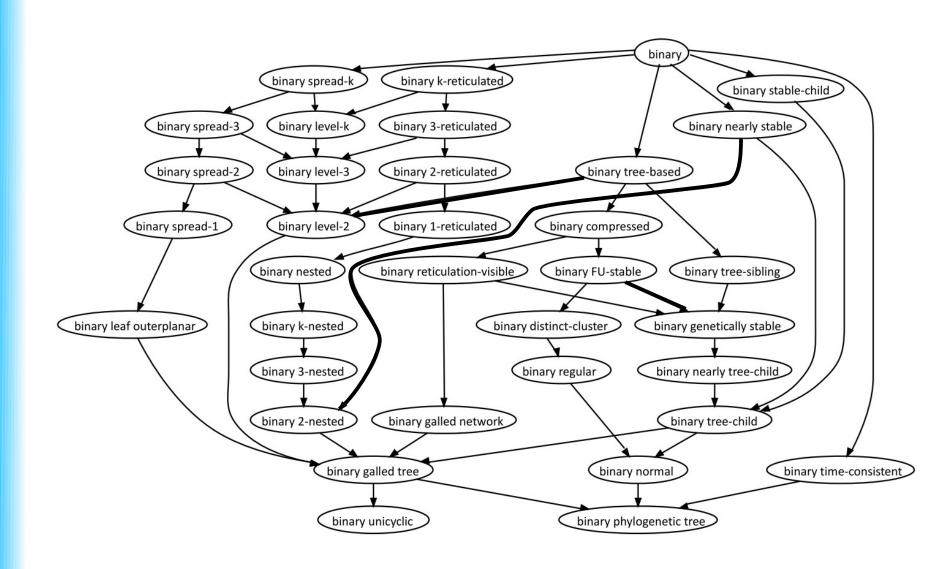


- <u>binary genetically stable</u>: All reticulation vertices are stable (e for leaf 2, d for leaf 1, g for leaf 3, j for leaf 4) and all have at least one parent which is stable (f, parent of d, stable for leaf 2; b, parent of e, stable for leaves 1 and 2; a, parent of g, stable for leaf 4)
- binary nearly stable: All vertices except c and i (whose unique parent is in both cases stable) are stable.
- binary level-2: Easy to check.
- binary leaf outerplanar: Easy to check.
- binary FU-stable: Easy to check.

#### Classes which do not contain this network (with direct proof)

- <u>binary nearly tree-child</u>: Reticulation vertex g is stable but none of its parents a and i have the tree-path property.
- · binary nested: Easy to check.
- binary time-consistent: The redundant arc from b to e makes it impossible to build a time-consistent labeling of the vertices.
- binary galled network: Reticulation arc (c,e) is a common arc of reticulation cycles from b to e and from c to d.
- binary distinct-cluster: Vertices h and i both have the same cluster: {3,4}
- binary 1-reticulated: Tree vertex b can reach 2 reticulation vertices by 2 directed internally vertex-disjoint paths: d and e.

joint work with Maxime Morgado and Narges Tavassoli http://phylnet.univ-mlv.fr/isiphync/network.php?id=4



### Classes of phylogenetic networks

#### Problems and properties studied on these classes

#### **Problems**

- Tree Containment: Does the input network contain the input tree on the same set of leaves?
- Cluster Containment: Does the input network contain the input subset of leaves as a softwired cluster?
- Phyloge netic Network Isomorphism: Are the two input phylogenetic networks isomorphic?

#### **Properties**

- Upper bound on the number of vertices: The number of vertices is bounded by the number of leaves.
- Unbounded number of vertices: The number of vertices is not bounded by the number of leaves.
- Completeness for reconstruction from trees: There exists a network in this class which displays all binary rooted phylogenetic trees on n leaves.

#### Database content

73 classes of phylogenetic networks including 35 classes of binary phylogenetic networks (defined in a total of 20 bibliographic references), 51 inclusion relationships proved directly between classes (including some found in a total of 9 bibliographic references), 21 networks (65 memberships to a class, 53 non-memberships to a class), 3 problems considered, 3 properties considered, 33 theorems proved directly (including some found in a total of 15 bibliographic references) including 23 positive results (which can be extended to subclasses) and 10 negative results (which can be extended to superclasses).

### Classes of phylogenetic networks

#### Problems and properties studied on these classes

#### **Problems**

- Tree Containment: Does the input network contain the input tree on the same set of leaves?
- Cluster Containment: Does the input network contain the input subset of leaves as a softwired cluster?
- Phyloge netic Network Isomorphism: Are the two input phylogenetic networks isomorphic?

#### **Properties**

- Upper bound on the number of vertices: The number of vertices is bounded by the number of leaves.
- Unbounded number of vertices: The number of vertices is not bounded by the number of leaves.
- Completeness for reconstruction from trees: There exists a network in this class which displays all binary rooted phylogenetic trees on n leaves.

#### Database content

73 classes of phylogenetic networks including 35 classes of binary phylogenetic networks (defined in a total of 20 bibliographic references), 51 inclusion relationships proved directly between classes (including some found in a total of 9 bibliographic references), 21 networks (65 memberships to a class, 53 non-memberships to a class), 3 problems considered, 3 properties considered, 33 theorems proved directly (including some found in a total of 15 bibliographic references) including 23 positive results (which can be extended to subclasses) and 10 negative results (which can be extended to superclasses).

**Polynomial time algorithm** available on class  $A \rightarrow$  works on **subclass** B **NP-completeness** on class  $B \rightarrow$  NP-completeness on **superclass** A (similar to ISGCI)

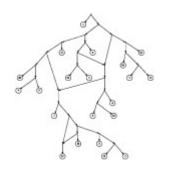
joint work with Maxime Morgado and Narges Tavassoli

#### **Outline**

- Phylogenetic networks
- Classes of phylogenetic networks
- The Tree Contaiment Problem

espèce 1 : AATTGCAG TAGCCCAAAAT
espèce 2 : ACCTGCAG TAGACCAAT
espèce 3 : GCTTGCCG TAGACAAGAAT
espèce 4 : ATTTGCAG AAGACCAAAT
espèce 5 : TAGACAAGAAT
espèce 6 : ACTTGCAG TAGCACAAAAT
espèce 7 : ACCTGGTG TAAAAT

G1 G2



#### {gene sequences}

#### distance methods

Bandelt & Dress 1992 - Legendre & Makarenkov 2000 - Bryant & Moulton 2002 - Chan, Jansson, Lam & Yiu 2006

#### parsimony methods

Hein 1990 - Kececioglu & Gusfield 1994 - Jin, Nakhleh, Snir, Tuller 2009 - Park, Jin & Nakhleh 2010 - Kannan & Wheeler. 2012

#### likelihood methods

Snir & Tuller 2009 - Jin, Nakhleh, Snir, Tuller 2009 -Velasco & Sober 2009 - Meng & Kubatko 2009

network N

# Problem: methods are usually slow, especially with rapidly increasing sequence length.

espèce 1 : AATTGCAG TAGCCCAAAAT
espèce 2 : ACCTGCAG TAGACCAAT
espèce 3 : GCTTGCCG TAGACAAGAAT
espèce 4 : ATTTGCAG AAGACCAAAT
espèce 5 : TAGACAAGAAT
espèce 6 : ACTTGCAG TAGCACAAAAT
espèce 7 : ACCTGGTG TAAAAT

G1 G2

{gene sequences}

#### distance methods

Bandelt & Dress 1992 - Legendre & Makarenkov 2000 - Bryant & Moulton 2002 - Chan, Jansson, Lam & Yiu 2006

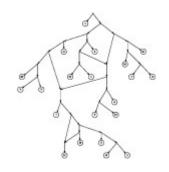
#### parsimony methods

Hein 1990 - Kececioglu & Gusfield 1994 - Jin, Nakhleh, Snir, Tuller 2009 - Park, Jin & Nakhleh 2010 - Kannan & Wheeler, 2012

#### likelihood methods

Snir & Tuller 2009 - Jin, Nakhleh, Snir, Tuller 2009 -Velasco & Sober 2009 - Meng & Kubatko 2009

network N



espèce 1 : AATTGCAG TAGCCCAAAAT espèce 3 : GCTTGCCG TAGACAAGAAT {gene sequences} espèce 4 : ATTTGCAG AAGACCAAAT espèce 6 : ACTTGCAG TAGCACAAAAT espèce 7 : ACCTGGTG TAAAAT Reconstruction of a tree for each gene present in several species Guindon & Gascuel, SB, 2003 {trees} **HOGENOM** Database Dufayard, Duret, Penel, Gouy, Rechenmann & Perrière, BioInf, 2005 Tree reconciliation or consensus explicit network optimal super-network N:

- contains the input trees

- has the smallest number of reticulations

espèce 1 : AATTGCAG TAGCCCAAAAT espèce 3 : GCTTGCCG TAGACAAGAAT {gene sequences} espèce 4 : ATTTGCAG AAGACCAAAT espèce 6 : ACTTGCAG TAGCACAAAAT espèce 7 : ACCTGGTG TAAAAT Reconstruction of a tree for each gene present in several species Guindon & Gascuel, SB, 2003 {trees} **HOGENOM** Database Dufayard, Duret, Penel, Gouy, Rechenmann & Perrière, BioInf, 2005 1470 species, >290 000 trees Tree reconciliation or consensus explicit network

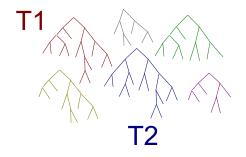
optimal super-network N:

- contains the input trees
- has the smallest number of reticulations

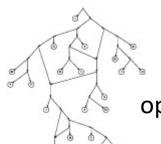
espèce 1 : AATTGCAG TAGCCCAAAAT espèce 2 : ACCTGCAG TAGACCAAT espèce 3 : GCTTGCCG TAGACAAGAAT espèce 4 : ATTTGCAG AAGACCAAAT espèce 5 : TAGACAAGAAT espèce 6 : ACTTGCAG TAGCACAAAAT espèce 7 : ACCTGGTG TAAAAT

G1

G2



explicit network



{gene sequences}

Reconstruction of a tree for each gene present in several species

Guindon & Gascuel, SB, 2003

{trees}

**HOGENOM** Database

Dufayard, Duret, Penel, Gouy, Rechenmann & Perrière, BioInf, 2005 1470 species, >290 000 trees

Tree reconciliation or consensus

**Tree Containment Problem** 

optimal super-network N:

- contains the input trees
- has the smallest number of reticulations

**Input:** A binary phylogenetic network *N* and

a tree *T* over the same set of taxa.

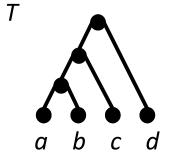
**Question:** Does *N* display *T*?

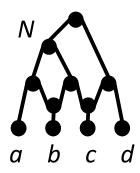
**Input:** A binary phylogenetic network *N* and

a tree T over the same set of taxa.

**Question:** Does *N* display *T*?

 $\rightarrow$  Can we remove one incoming arc, for each vertex with >1 parent in N, such that the obtained tree is equivalent to T?



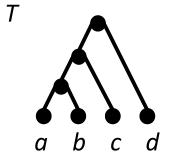


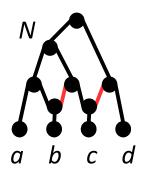
**Input:** A binary phylogenetic network *N* and

a tree T over the same set of taxa.

**Question:** Does *N* display *T*?

 $\rightarrow$  Can we remove one incoming arc, for each vertex with >1 parent in N, such that the obtained tree is equivalent to T?





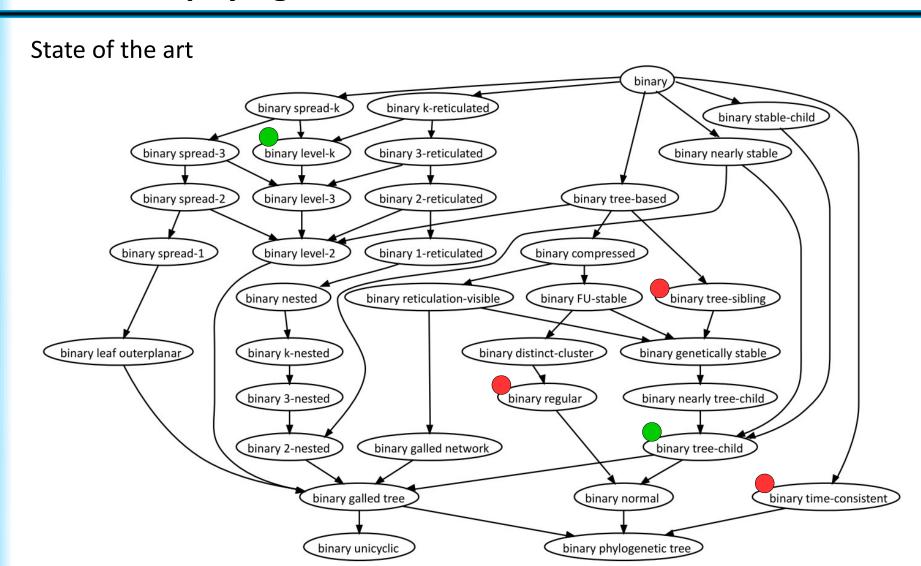
**Input:** A binary phylogenetic network *N* and

a tree T over the same set of taxa.

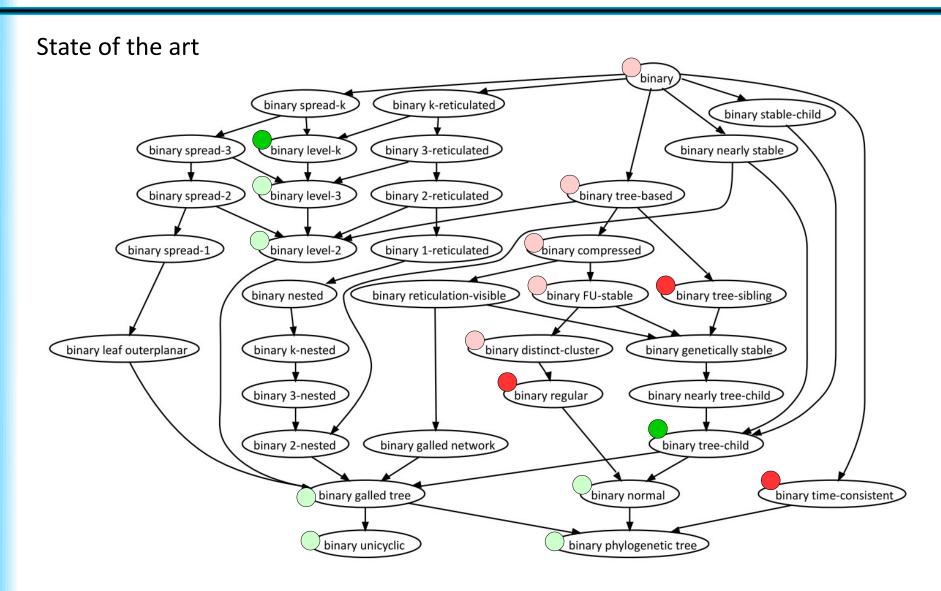
**Question:** Does *N* display *T*?

- NP-complete in general (Kanj, Nakhleh, Than & Xia, 2008)
- NP-complete for tree-sibling, time-consistent, regular networks (lersel, Semple & Steel, 2010)
- Polynomial-time solvable for normal networks, for binary tree-child networks, and for level-k networks (Iersel, Semple & Steel, 2010)

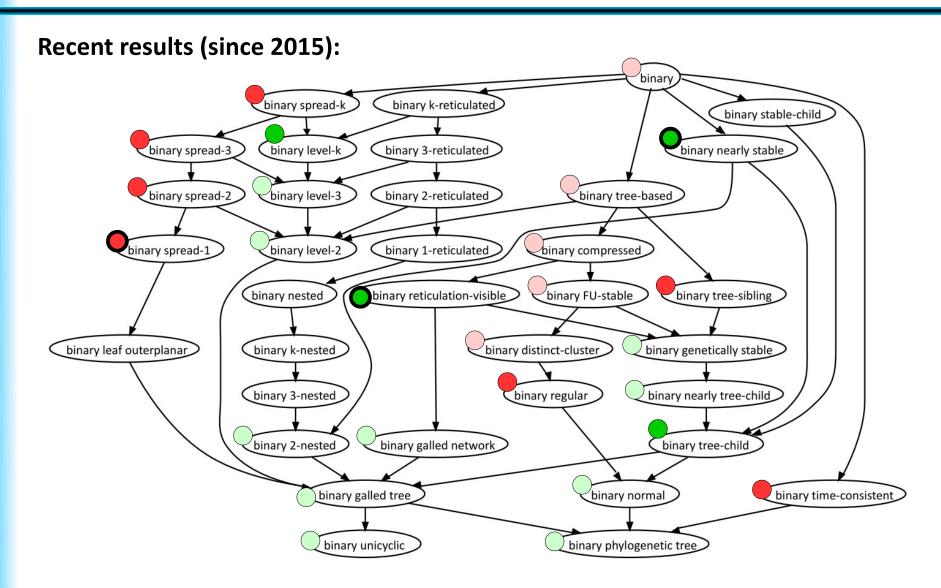
# Classes of phylogenetic networks and the T.C.P.



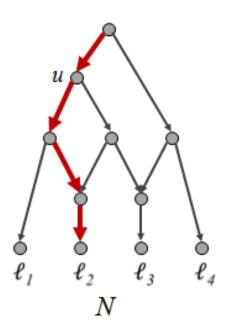
## Classes of phylogenetic networks and the T.C.P.



## Classes of phylogenetic networks and the T.C.P.



# Reticulation-visible and nearly-stable networks



A vertex *u* is **stable** if there exists a leaf *l* such that all paths from the root to *l* go through *u*.

A phylogenetic network is **reticulation-visible** if every reticulation vertex is stable.

A phylogenetic network is **nearly-stable** if for each vertex, either it is stable or its parents are.

## Strategy to get a quadratic time algorithm for T.C.P.

Given N, a phylogenetic network with n leaves and the input tree T of the T.C.P.

**Theorem 1:** If N is reticulation-visible then:  $\#\{\text{reticulation vertices of } N\} \le 4(n-1) \\ \#\{\text{vertices of } N\} \le 9n$ 

**Theorem 2:** If N is nearly-stable then  $\#\{\text{reticulation vertices of } N\} \le 12(n-1)$ 

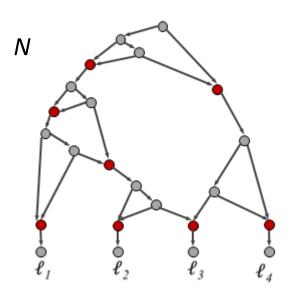
- **Theorem 3:** Considering a longest path in *N* (nearly stable), it is possible, in constant time:
  - either to realize that T is not contained in N
  - or to build a network N' with less arcs than N such that
     T contained in N if and only if T contained in N'

#### Decompose *N* into **2***n***-2 paths**:

- remove one reticulation arc per reticulation, ensuring we get no « dummy leaf », to get a tree *T* with *n* leaves
- summarize T into a rooted binary tree T' with n leaves... and 2n-2 arcs

We can prove (technical) that:

each path contains at most 2 reticulation vertices

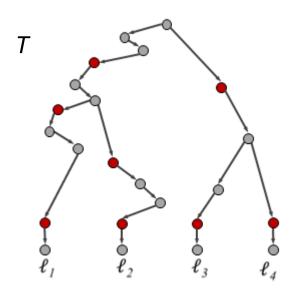


#### Decompose *N* into **2***n***-2 paths**:

- remove one reticulation arc per reticulation, ensuring we get no « dummy leaf », to get a tree *T* with *n* leaves
- summarize *T* into a rooted binary tree *T'* with *n* leaves... and 2*n*-2 arcs

We can prove (technical) that:

each path contains at most 2 reticulation vertices

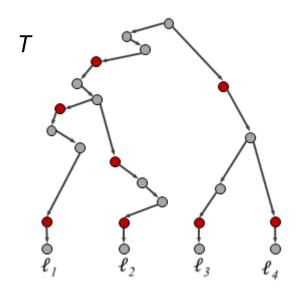


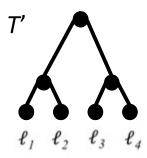
#### Decompose *N* into **2***n***-2 paths**:

- remove one reticulation arc per reticulation, ensuring we get no « dummy leaf », to get a tree T with n leaves
- summarize T into a rooted binary tree T' with n leaves... and 2n-2 arcs

We can prove (technical) that:

each path contains at most 2 reticulation vertices





Decompose *N* into **2***n***-2 paths**:

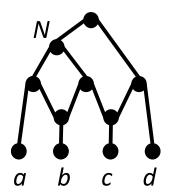
- remove one reticulation arc per reticulation, ensuring we get no « dummy leaf », to get a tree *T* with *n* leaves
- summarize T into a rooted binary tree T' with n leaves... and 2n-2 arcs

We can prove (technical) that:

each path contains at most 2 reticulation vertices

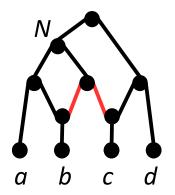
 $\rightarrow$  N contains at most 4(n-1) reticulation vertices

« Dummy leaves »?

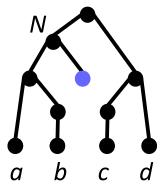


Deleting reticulation arcs can create « dummy leaves »

« Dummy leaves »?



Deleting reticulation arcs can create « dummy leaves »

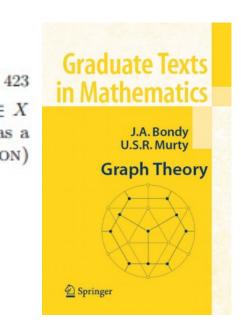


Possible to avoid creating « dummy leaves »?

Possible to avoid creating « dummy leaves »?

16.2 Matchings in Bipartite Graphs

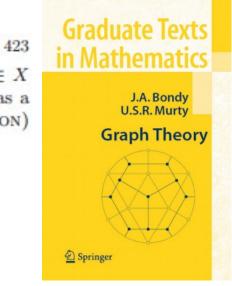
**16.2.13** Let G := G[X, Y] be a bipartite graph such that  $d(x) \ge 1$  for all  $x \in X$  and  $d(x) \ge d(y)$  for all  $xy \in E$ , where  $x \in X$  and  $y \in Y$ . Show that G has a matching covering every vertex of X.

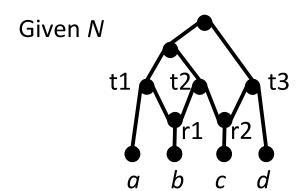


Possible to avoid creating « dummy leaves »?

16.2 Matchings in Bipartite Graphs

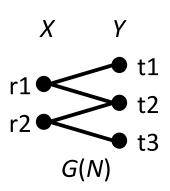
**16.2.13** Let G := G[X, Y] be a bipartite graph such that  $d(x) \ge 1$  for all  $x \in X$  and  $d(x) \ge d(y)$  for all  $xy \in E$ , where  $x \in X$  and  $y \in Y$ . Show that G has a matching covering every vertex of X.





Build G(N), bipartite graph such that:

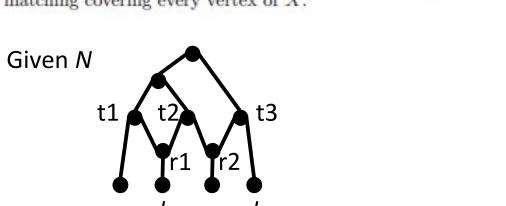
- X = reticulation vertices of N
  - $\rightarrow$  all vertices in X have degree 2
- Y = tree vertices of N with at least one reticulation child
  - $\rightarrow$  all vertices in Y have degree 1 or 2
- edge between x and y iff x is a child of y

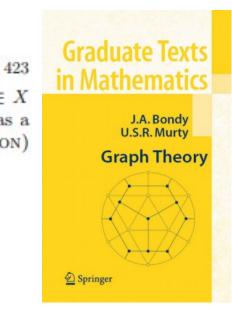


Possible to avoid creating « dummy leaves »?

16.2 Matchings in Bipartite Graphs

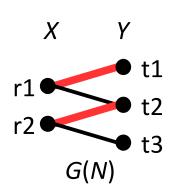
**16.2.13** Let G := G[X, Y] be a bipartite graph such that  $d(x) \ge 1$  for all  $x \in X$  and  $d(x) \ge d(y)$  for all  $xy \in E$ , where  $x \in X$  and  $y \in Y$ . Show that G has a matching covering every vertex of X.





Build G(N), bipartite graph such that:

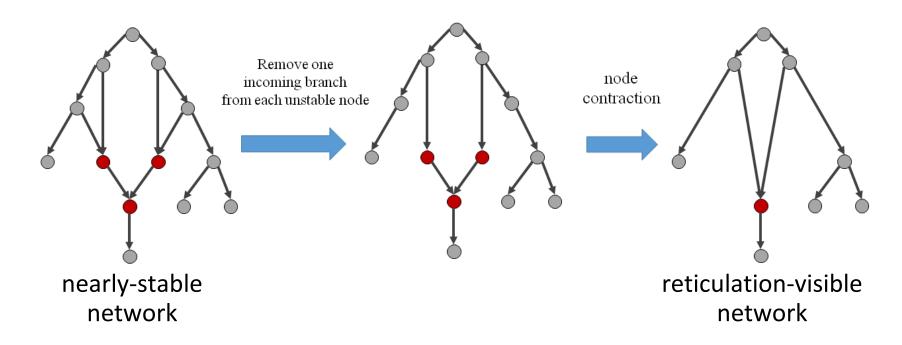
- X = reticulation vertices of N
  - $\rightarrow$  all vertices in X have degree 2
- Y = tree vertices of N with at least one reticulation child
  - → all vertices in Y have degree 1 or 2
- edge between x and y iff x is a child of y



 $\rightarrow$  matching covering every vertex of  $X \rightarrow$  edges to remove from N

# Number of reticulations of a nearly-stable network

Reduce nearly-stable networks to stable networks



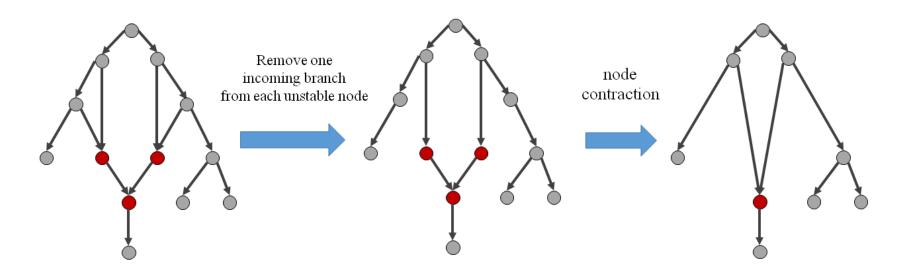
**Claim:** #unstableReticulations ≤ 2 #stableReticulations

#### **Proof:**

Each unstable reticulation must have a stable reticulation child. At most two unstable reticulations may have the same reticulation child.

# Number of reticulations of a nearly-stable network

Reduce nearly-stable networks to stable networks



#unstableReticulations ≤ 2 #stableReticulations

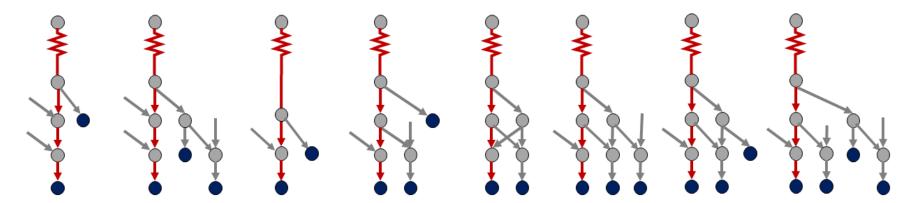
#stableReticulations  $\leq 4(n-1)$ 

 $\rightarrow$  #reticulations  $\leq 12(n-1)$ 

## Deleting reticulation arcs to simplify the question

Simplify N by removing an arc near the end of a longest path P.

Case analysis (8 cases):



#### Algorithm for nearly-stable networks:

#### Repeat:

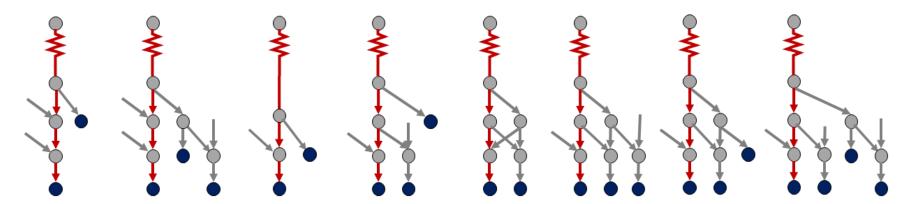
- Compute a longest path P in N
- Simplify N by considering the subnetwork at the end of P according to the 8 cases above (arc removal + contraction)
- Replace a «cherry» (2 leaves + their common parent)
   appearing in both N and T by a new leaf

Finally check that the obtained network is identical to T

## Deleting reticulation arcs to simplify the question

Simplify N by removing an arc near the end of a longest path P.

Case analysis (8 cases):



#### Algorithm for nearly-stable networks:

R	6	n	6	ล	t	•
	_	Μ	_	ч	·	•

- Compute a longest path P in N
- Simplify N by considering the subnetwork at the end of P according to the 8 cases above (arc removal + contraction)
- Replace a «cherry» (2 leaves + their common parent) appearing in both N and T by a new leaf

Finally check that the obtained network is identical to T

### O(n) times:

- $\rightarrow O(n)$
- $\rightarrow$  O(1)
- $\rightarrow$  O(1)

 $\rightarrow$  O(n)

### Improved algorithms

 $O(n \log n)$ -time algorithm for nearly-stable networks

Fakcharoenphol, Kumpijit & Putwattana, JCSSE 2015

Cubic-time algorithm for reticulation-visible networks

Gunawan, DasGupta & Zhang, RECOMB 2016 Bordewich & Semple, Advances in Applied Mathematics, 2016

#reticulations  $\leq 3(n-1)$  for reticulation-visible networks

Bordewich & Semple, Advances in Applied Mathematics, 2016

### Perspectives...

- Provide a practical algorithmic toolbox using network classes
  - → http://phylnet.info/tools/
- Combine the combinatorial and statistical approaches to reconstruct phylogenetic networks
  - → CNRS PICS project with L. van Iersel, S. Kelk, F. Pardi & C. Scornavacca
- Develop interactions with related fields:
  - → host/parasite relationships
  - → population genetics
  - → stemmatology