THE DIFFERENTIAL TOPOLOGY OF COMBINATORIAL SPACES

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Abstract

We will show how many ingredients from the study of smooth manifolds, such as vector fields, flows, and Morse Theory (along with its generalizations and extensions), can be used effectively in the investigation of simplicial complexes and other combinatorial spaces.

(The items marked with a (*) are the most suitable for getting an introduction to the subject.)

References

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